

# Mathematical Model of PV Cell Module in Matlab

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## Abstract

The physical modeling of the system is not that much efficient so the analysis is done through the mathematical modeling approach. In this paper mathematical analysis is done for the single diode model. Single diode model is employed to investigate the I-V and P-V characteristics of 46 W module. The effect of irradiation and temperature is also considered. The analysis is done in MATLAB/SIMULINK environment. This mathematical analysis approach is a very flexible to change the Parameters of the system.

## Keywords

Solar Energy, Photo Voltaic Effect, MATLAB/SIMULINK, Characteristics of PV cell.

## PV Cell Modelling

For computer simulation of a physical system modeling should be done. It includes all the physical elements & all the parameters influencing the system. In this dealing the physical system is converted to computer codes and characteristics are plotted. To describe the behavior of the physical PV cell, the PV model is chosen by the researchers. Most commonly used model is a single diode model

## I. Introduction

Conventional energy sources are unable to meet the increasing demand for energy worldwide. So, alternative energy sources like sunlight, wind and biomass come into picture. In that context, photovoltaic energy is a source of interesting energy; it is renewable, inexhaustible and non-polluting, and it is used as energy sources in various applications [10]. But because of its high cost and low efficiency, energy contribution is less than other energy sources. It is therefore essential to have effective and flexible models, to enable you to perform easy manipulation of certain data (irradiance and temperature) investigate how to get its performance as maximum as possible. The use of these simple models provides sufficient accuracy to analyze the behavior of the solar cell and have proven to be effective in most cases. Solar cells convert solar energy into electrical energy. This phenomenon occurs in materials which have the property of capture photon and emit electrons. The main material used in the photovoltaic industry is silicon. For the better understanding of the PV module the mathematical model is continuously updated. The output characteristics of PV module depends on

- The solar Isolation.
- The cell Temperature and
- The Output Voltage of PV Module.

It is necessary to model the PV module for the design and simulation of Maximum power point tracking for PV system applications because it has non-linear characteristics. Mathematical modelling of the solar array (module) here is done mainly for obtaining the performance characteristics. The performance characteristics of PV module mainly depend on the operating conditions, they also depend on solar array design quality.

The output quantities (Voltage, current and power) vary as a function of irradiation, temperature and load current. The effects of these three variations are considered in the modeling, so that any change in the temperature and solar irradiation levels should not adversely affect the PV module output. The Photo voltaic analysis model proposed in this paper is circuitry based model to be used with simulink. Here module is modelled and P-V & I-V characteristics are plotted for different irradiation (1000W/m<sup>2</sup>, 600W/m<sup>2</sup>, 200W/m<sup>2</sup>) and for different temperatures (250 C, 500C and 750 Introduction

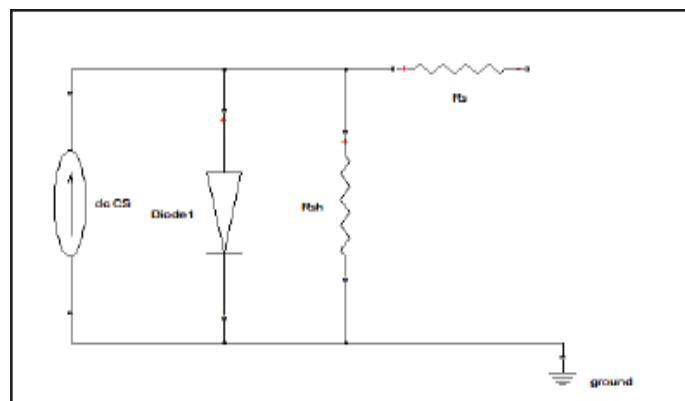


Fig. 1: Solar Cell Model

Electron-hole pairs are created, when light falls at the junction and it provides an electrical current flow across the junction of constant rate. Then net current is calculated by considering difference between the normal current and light generated current. The internal series Resistance  $R_s$  is in series with the junction. It is mostly d

## II. Principle and Operation of PV Cell

An array/module of pv cell converts solar energy into a usable amount of DC (direct current) energy. The panels of solar made of semiconductor. Material and silicon being the most abundant (very large) used semiconductor [1].

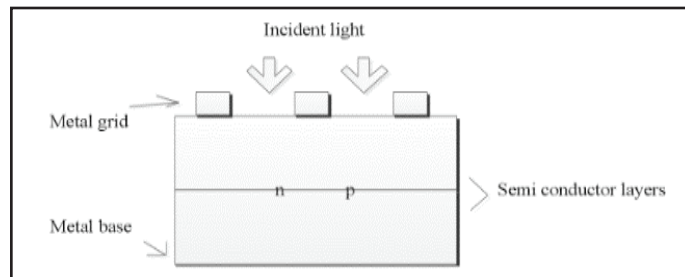


Fig. 2: Physical Structure of PV Cell

The p-n junction exposed to light, photons with energy greater than the gap of energy are absorbed, causing the emergence of electron-hole pairs. These carriers are separated under the influence of electric fields within the junction. Creating a current that is proportional to incidence of solar irradiation [3]. Being exposed to the sunlight, photons with energy of the semiconductor creates some electron-hole pair proportional to the incident irradiation

[4]. The light generated current is acted as a constant current source supplying the current to either the junction or a useful load depending on the junction characteristics and the value of the external load resistance. This phenomenon depends on the semiconductor material and on the wavelength of the incident light. The rate of generation of electric carriers depends on the flux of incident light and the capacity of absorption of semiconductor. The capacity of absorption depends mainly on the semiconductor band gap, on the reflectance of the cell surface (that depends on the shape and treatment of the surface). The value of series resistance is very low, but the value of parallel resistance is infinity.

### III. Characteristics of PV Cell

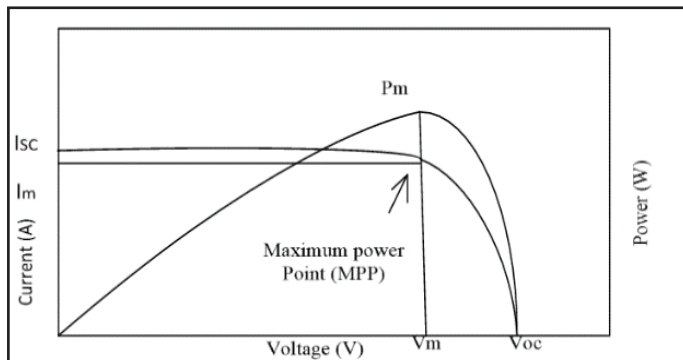


Fig. 3:

That may be increase or decrease output power due to all parameters used in pv cell like irradiation, temperature, series resistance, parallel resistance, ideality factor, saturation current etc. due to the high sheet resistance of the diffused layer which is in series with the junction properties. Studies in this field indicate that exploiting Nano fluid in solar systems, offers unique advantages over conventional fluids. In this paper, the applications of nanofluids on different types of solar collectors, photovoltaic systems and solar thermoelectric are reviewed. Beside the wide range of energy conversion, the efforts done on the Energy Storage System (ESS) have been reviewed. In the field of economics, nanotech reduces manufacturing costs as a result of using a low temperature process. Research is needed for better understanding the effects from the Low pass and high pass and band pass width

### IV. Mathematical Modeling of PV CELL

The equivalent circuit diagram of pv cell is shown below in figure. It includes a current source ( $I_{ph}$ ), diode (D), a series resistance ( $R_s$ ), and shunt resistance ( $R_{sh}$ ) [2].

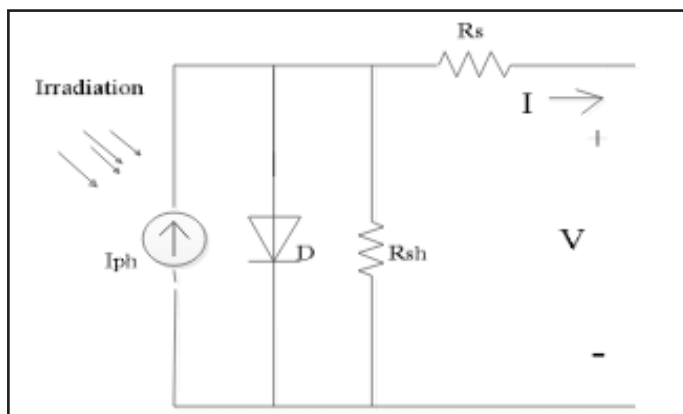


Fig. 4: Circuit Diagram of pv Cell

The equivalent circuit based model is mainly used for the MPPT technologies. In mathematical equations in pv cell/module used following nomenclature.  $V_{pv}$  is the output voltage,  $I_{pv}$  is output current,  $T_n$  is the reference temperature  $T$  is the operating temperature in Kelvin  $I_s = I_0$  is the saturation current (A)  $I_{sc}$  is the short circuit current  $I_0 R$  is the cell reverse saturation current at a reference temperature  $I_{ph}$  is the light generated current or photon current  $A=B$  is the ideality factor  $K$  is the Boltzmann constant ( $1.3805 \times 10^{-23}$  J/K)  $q$  is electron charge ( $1.6 \times 10^{-19}$  C)  $R_s$  is the series resistance  $R_{sh}$  is the shunt resistance  $N_s$  is the number of cells connected in series  $N_p$  is the number of cells connected in parallel is the band gap energy (1.1 eV)  $K_i$  is a cell's short circuit temperature coefficient  $G$  is the irradiance ( $W/m^2$ ) The voltage, current ( $V-I$ ) characteristic equation of pv/solar cell is given by

$$I = I_{ph} - I_0 \left( \exp \frac{q(V+IR_s)}{NKT} - 1 \right) - \frac{(V+IR_s)}{R_{sh}} \quad (1)$$

Where photon current is-

$$I_{ph} = (I_{sc} + K_i (T - T_n)) \frac{G}{100} \quad (2)$$

The cell's saturation current varies with cell temperature, which is-

$$I_{s(T)} = I_s \left( \frac{T}{T_n} \right)^3 \exp \left[ \frac{E_g}{V_t} \left( \frac{T}{T_n} - 1 \right) \right] \quad (3)$$

$V_t$  is called thermal voltage-

$$V_t = K \cdot T / q \quad (4)$$

The current output of pv module is-

$$I_{pv} = N_p \cdot I_{ph} - N_p \cdot I_0 \left[ \exp \left\{ \frac{q \cdot (V_{pv} + I R_s)}{N_s \cdot A \cdot K T} \right\} - 1 \right] \quad (5)$$

### V. Maximum Power Point Tracking

MPPT is an algorithm that included in charge controllers used for extracting maximum available power from pv cell/module under certain conditions. This voltage at which pv cells/module can provide maximum power is called maximum power point (or peak power voltage) [11]. The output power depends on it radiation, temperature and its parameters and product of voltage and current

#### A. Perturb and Observe (P&O) Method

P&O is mostly used algorithm for MPPT. And it operated by the periodically perturbing (increasing or decreasing). It involves introducing perturbation in power operating voltage. In this algorithm if the power has increased, it keeps same direction (increase voltage) otherwise, changes its direction (decrease voltage). This process is repeated at each MPP tracking step until the MPP is reached. After reaching the MPP, the algorithm naturally oscillates around its correct value. It means power decreases then continue vary the voltage or current in the reverse direction.

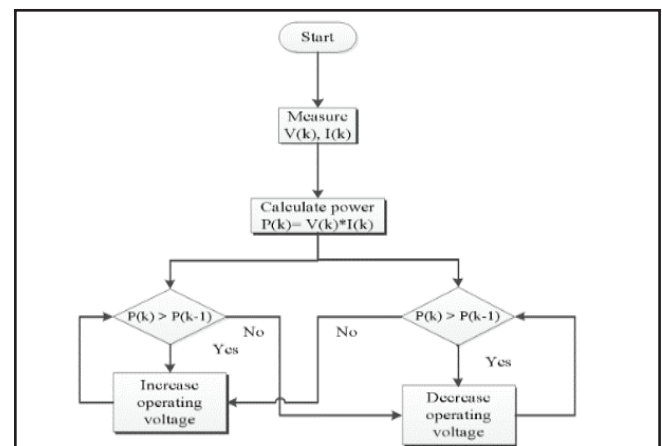


Fig. 5: Flow Chart for P&O Method

### Incremental Conductance Method

The P&O method is not sufficient for all condition of the MPP, and it fail under continues changing environment condition. So overcome this condition we use incremental conductance method. In this method used to derivative of the current with respect to the voltage to reach the maximum power point (MPP). This maximum power should be equal to  $\frac{dP}{dV} = 0$

The variation in the voltage towards biggest or smallest value it also be affected the power value. If power increase then should continue in the same direction. If power decrease then should be reverse direction

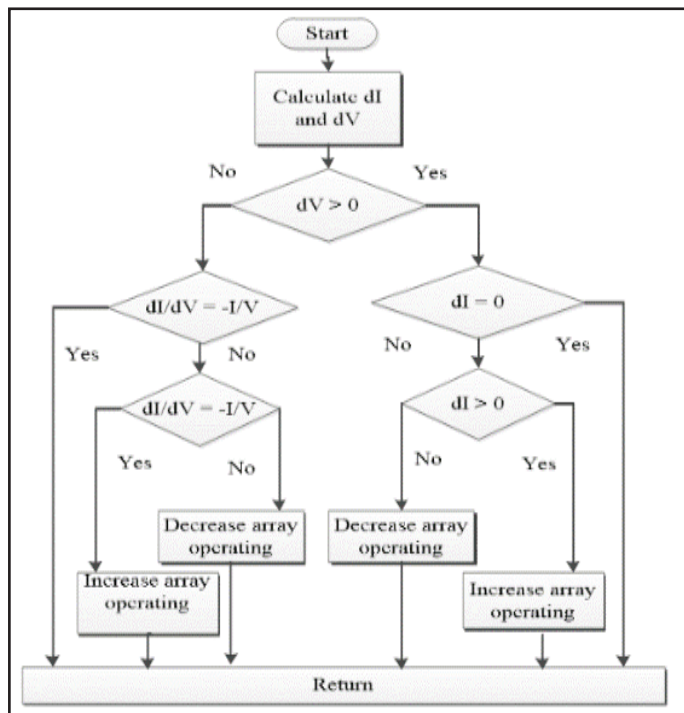


Fig. 6: Flow Chart of Interemental Conductance Method

### VI. Simulink PV Model

The blocks of the model are developed using MATLAB/Simulink based on mathematical equations [5]. The photovoltaic model and circuits that can be used in simulation of power conversion for its applications and shows the different conditions related to physical and environmental to estimate the electrical behavior of the pv cell [9] The simulation model of photo current ( $I_{ph}$ ) as shown in below-

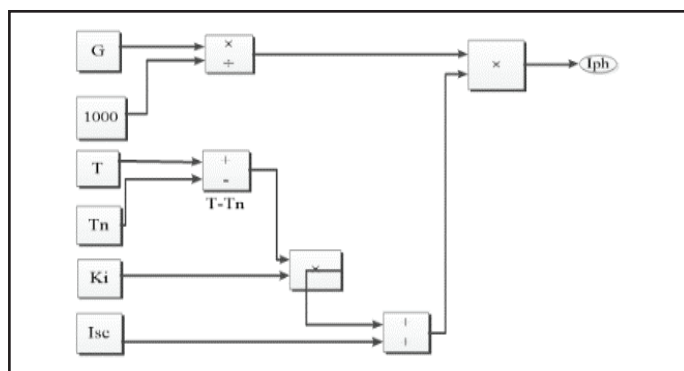


Fig. 7: Simulation Model of Calculation of  $I_{ph}$

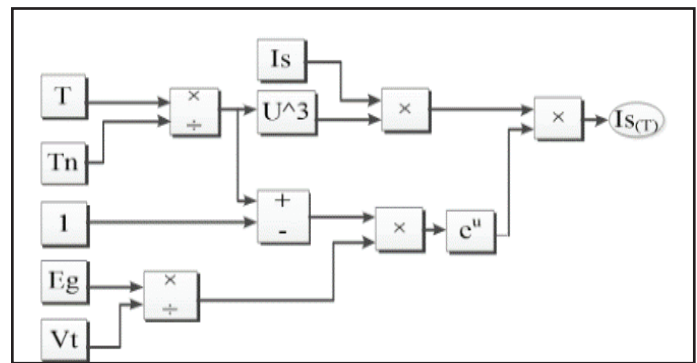


Fig. 8: Simulink Model of Reverse Saturation Current

### VII. Conclusion

A pv model based on the mathematical equation of solar cell is developed using MATLAB/Simulink model. In pv array works only part of the I-V characteristic near the working point maximum voltage and current. The photovoltaic system works most of time with maximum efficiency. The behavior of the pv cell in electrical changes in the varies parameters like resistance, sun irradiation, temperature, and parameter of the diode are value considered as input and the I-V and P-V characteristics are considered to output. Increasing temperature yields decreasing power and voltage and increasing sun irradiation the current and voltage and also power will be increased. Parallel resistance, no significant effect or (little effect) on the I-V and P-V curve if change of resistance has a very low effect on power. Soremoving it to have a simple model, and increasing the series resistance results in the decreasing the power, increasing the diode ideality factor power is increased, while and increasing the amount of reverse saturation current power will reduce. In the paper two techniques (P&O, incremental conductance method) used to maximize the output power. By analyzing the current with the help of mathematical model it has very convenient justified, required parameters by changing the value.

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